

## What Pieces of Limit Order Book Information Matter in Explaining Order Choice by Patient and Impatient Traders?

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# What Pieces of Limit Order Book Information Matter in Explaining Order Choice by Patient and Impatient Traders?

## ABSTRACT

In this paper, we extend the existing empirical evidence on the relationship between the state of the limit order book (LOB) and order choice. Our contribution is twofold: first, we propose a sequential ordered probit (SOP) model which allows studying patient and impatient traders' choices separately; second, we consider two pieces of LOB information, the best quotes and the book beyond the best quotes. We find that both pieces of LOB information explain the degree of patience of an incoming trader and, afterwards, its order choice. Nonetheless, the best quotes concentrate most of the explanatory power of the LOB. The shape of the book beyond the best quotes is crucial in explaining the aggressiveness of patient (limit order) traders, while impatient (market order) traders base their decisions primarily on the best quotes. Patient traders' choices depend more on the state of the LOB on the same side of the market, while impatient traders mostly look at the state of the LOB on the opposite side. The aggressiveness of both types of traders augments with the inside spread. However, patient (impatient) traders submit more (less) aggressive limit (market) orders when the depth of the own (opposite) best quote and the length of the own (opposite) side of the book increase. We also find that higher depth away from the best ask (bid) quote may signal that this quote is "too low (high)", causing incoming impatient buyers (sellers) to be more aggressive and incoming patient sellers (buyers) to be more conservative.

**Key words:** Limit orders, market orders, limit order book, order aggressiveness, order-driven markets.

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# 1. Introduction

In order driven markets without designated market makers, liquidity relies on the submission of limit orders. Limit orders are stored on an electronic register, called the (open) limit order book (henceforth, LOB), to wait for execution. To appreciate how and why liquidity varies over time in these venues, it is first necessary to comprehend the forces leading an incoming investor to decide between submitting a limit order (liquidity supply) or a market order (liquidity demand). Some recent studies illustrate that informed and uninformed investors order choices also happen to be essential to understand how new information is incorporated into prices (e.g., Harris, 1998, Anand et al., 2005, Bloomfield et al., 2005). It has also been shown that order choice determines the speed and costs (quality) of execution (e.g., Harris and Hasbrouck, 1996; Lo et al., 2002, and Al-Suhaibani and Kryzanowski, 2000). Finally, the growing interest in the optimization of order submissions, an underlying foundation of algorithm trading (see O’Hara, 2007), also corroborates the relevance of this topic in microstructure research.

Quite a few recent theoretical studies have evaluated the role the LOB plays in order choice. In the dynamic models of Parlour (1998), Foucault (1999), Handa et al. (2003), Foucault et al. (2005), Goettler et al. (2005), and Rosu (2005), LOB dimensions, such as the quoted depth on both sides of the LOB and the inside spread, determine the choice between market and limit orders. This theoretical interaction between the state of the LOB and the traders’ order choices has been extensively corroborated by the empirical literature (e.g., Biais et al., 1995; Griffiths et al., 2000; Al-Suhaibani and Kryzanowski, 2000; Rinaldo, 2004; Beber and Caglio, 2005, and Ellul et al., 2007).<sup>1</sup>

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<sup>1</sup> All this theoretical and empirical literature is revised in detail in the next section.

This paper is aimed to contribute to this literature. Our approach differs from previous empirical studies in two main aspects. First, we propose a two-stage *sequential* ordered probit (henceforth SOP) model, instead of the more commonly used ordered probit model (e.g., Griffiths et al., 2000; Ranaldo, 2004), to model order aggressiveness. The SOP model allows studying patient and impatient order choices separately. In the first stage of our model, the trader defines herself as patient or eager, as she must choose between removing, providing and consuming liquidity, without specifying a particular type or order. In most of the previously cited theoretical models on order choice, the degree of patience of an incoming trader is exogenously given (by factors such as her degree of risk aversion, a higher or lower discount rate, her waiting costs, her liquidity needs, or her access to perishable non-publicly known information). In equilibrium, patient traders tend to submit limit orders while impatient traders tend to submit market orders (e.g., Foucault et al., 2005, and Rosu, 2005). However, these models also postulate that the state of the LOB may have an influence in reshaping their degree of patience, leading to unanticipated order choices.<sup>2</sup> In our empirical analysis, we identify patient and impatient traders based on posterior order choices. In this first stage of our SOP model, we therefore evaluate the importance of the LOB in determining the character of an incoming trader.

In the second stage of the SOP model, the trader chooses among the different types of orders available given their predetermined disposition. Thus, a patient trader chooses among the different types of limit orders, either away from, at, or within the best quotes. In this decision, the patient trader faces a direct tradeoff between a more favorable limit price and a higher risk of non-execution. The impatient trader, though, has to fix the

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<sup>2</sup> Recent empirical and theoretical research (see Kaniel and Liu, 2006; Harris, 1998; Bloomfield et al., 2005, and Anand et al., 2005) has shown that, under certain circumstances, traders that are presumed to be more inclined to be impatient, such as informed traders, may choose to submit orders that a priori are more appropriate for patient traders.

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2  
3 relative size of her order. She must choose between a market order that requests less  
4 than available, all that is available, or more volume than available at the best opposite  
5 quote. This decision determines the instantaneous price impact of the trade and the  
6 average immediacy cost per share. Hence, in this second stage, we evaluate the  
7 relevance of the LOB in the decision of choosing a particular type of order by each  
8 particular type of trader.  
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18 Second, we contribute to the literature by providing empirical evidence on how the  
19 state of the LOB beyond the best quotes affects order choices. We understand the LOB  
20 as a set of two main pieces of information, the best quotes and the book beyond the best  
21 quotes. This distinction is not arbitrary, since even some of the most pre-trade opaque  
22 markets provide information about the best quotes. Additionally, most of the above-  
23 cited theoretical papers focus on modeling order choice conditional on the best quotes.  
24 The exception is Goettler et al. (2005). Using simulations, they postulate different  
25 effects of both pieces of LOB information on order choice by both patient and impatient  
26 traders. In this paper, we provide empirical evidence confirming many of their  
27 simulation findings.<sup>3</sup> Moreover, previous empirical papers about order aggressiveness  
28 only consider the best quotes of the LOB. Relevant exceptions are Irvine et al. (2000)  
29 and Cao et al. (2003). Irvine et al. (2000) show that a liquidity measure based on LOB  
30 data is more informative about subsequent order flow than the traditional measures  
31 based on the best quotes. Cao et al. (2003) examine the informativeness of the LOB  
32 beyond its first level. They conclude that the best quotes lead price discovery and  
33 provide a better estimator of the true value, but the information derived from the  
34 secondary level of the book adds some “marginal” explanatory power on future returns.  
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<sup>3</sup> Rosu (2005) also considers the whole LOB in his theoretical model. In this case, however, there are no clear cut predictions regarding best quotes versus the book beyond the best quotes.

Although our paper inevitably overlaps with Cao et al.'s (2003) paper at some point, the motivations and methods differ since they focus on price discovery.

We use high frequency LOB data on the Stock Exchange Interconnection System of the Spanish Stock Exchange (henceforth SSE). In this market, the LOB is available in real time to all market participants and market orders are not restricted to the best quotes. Hence, the shape of the entire LOB, and not only the best quotes, determines the immediacy costs of a market order, as well as the expected time-to-execution of a limit order.

Our main findings are as follows. Consistently with previous empirical studies, we find that the state of the LOB matters in explaining the aggressiveness of incoming traders. Additionally, we show that both the best quotes and the book beyond the best quotes help to shape the degree of patience of incoming buyers and sellers, though most of this effect is due to the best quotes. When we look at patient and impatient traders separately, we report asymmetric patterns. Thus, incoming patient traders strongly rely on the state of the book beyond the best quotes, while impatient traders base their strategic decisions primarily on the prevailing best quotes. Both patient and impatient traders condition the placement of their limit orders on the inside spread. However, patient (impatient) traders' choices rely on the depth at and away from the best quote and the length of the book on the same (opposite) side of the market. Consistently with Goettler et al. (2005), our evidence shows that higher depth away from the best ask (bid) quote may signal that this quote is "too low (high)", causing incoming impatient buyers (sellers) to place market orders more aggressively and incoming patient sellers (buyers) to place limit orders more conservatively. Finally, we show that our SOP model provides better in sample and out of sample goodness-of-fit performance than the traditional ordered probit model of order aggressiveness.



The paper proceeds as follows. In the next section, we briefly review the pertinent literature. In section 3, we introduce the two-stage SOP model and discuss several methodological details. In section 4, we describe the database, the sample, and the market. In section 5, we present our empirical findings. Finally, in section 6, we conclude.

**2. Literature review**

Cohen et al. (1981), Copeland and Galai (1983), and Handa and Schwartz (1996) set the basic rationale for limit order trading as a trade-off between the non-execution costs and the picking-off risk carried by limit orders, and the immediacy costs supported by market orders. Other things being equal, the lower the non-execution risk and the higher the immediacy costs, the more likely the incoming trader is to submit a limit order. Moreover, an increase in adverse selection costs aggravates the winner’s curse problem faced by uninformed limit order traders.

Recent theoretical developments suggest that the state of the LOB may be critical to order choice. Parlour (1998) proposes a dynamic equilibrium model in which the thickness of a given side of the LOB produces a “crowding out” effect on the limit orders on that side, because of the long expected time-to-execution. In contrast, traders on the opposite side, anticipating the crowding out effect, are better submitting less aggressive orders.

Foucault (1999) develops a dynamic limit order market in which the mix between market and limit orders in equilibrium depends on the fundamental volatility of the stock. When volatility increases, the risk of being picked-off by an informed trader increases. Limit order traders respond posting higher ask prices and lower bid prices.

This makes market orders less attractive and, consequently, the proportion of limit orders on the total order flow increases.

Foucault et al. (2005) develop a dynamic model for an order driven market populated by strategic liquidity traders that differ in their waiting costs. In this model, order choice is determined by the bid-ask spread, but not by quoted depth.<sup>4</sup> For certain spread levels, patient (low waiting costs) traders tend to place limit orders, while impatient (high liquidity costs traders) tend to submit market orders. As the spread increases and surpasses a certain cutoff level, however, all traders tend to choose limit orders to trade. Moreover, liquidity suppliers are willing to offer larger spread improvements when the spread is large.

Rosu (2005) proposes a continuous time version of the latter model where competition between limit order traders generates endogenous undercutting. The whole shape of the LOB is considered, not only the best quotes. By allowing market orders of different sizes with probabilities which do not decrease too fast with order size, the author shows that limit orders may cluster away from the best quotes. Moreover, traders are allowed to dynamically cancel and resubmit their orders as the shape of the LOB changes over time. When the LOB is full, “fleeting” orders may happen: a patient trader submits a limit order inside the quotes and an opposite patient trader accepts it immediately by canceling her limit order and placing a market order.

In Goettler et al. (2005), liquidity motivated traders with differing degree of patience choose whether to buy or sell (or both), either using limit orders or market orders (or both), given the state of the LOB and a consensus true value. Traders who are eager to buy (sell) are allowed to submit limit orders above (below) the consensus value, which

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<sup>4</sup> This arises because limit order submitters are not allowed to submit orders at or away from the best quotes.

means that market orders may result in negative transaction costs. Because the consensus value can change, limit orders suffer from picking-off risk. All else equal, the higher the probability of execution and the lower the picking-off risk at some price, the higher the number of limit orders to sell (buy) submitted at that price. Using simulations, they find that, when the spread is wide, a thicker best bid increases (decreases) the frequency of inside-the-quotes limit (market) orders to buy. Additionally, higher depth above (below) the best ask (bid) quote may signal that the best quote may be “too low (high)” resulting in a more aggressive (conservative) order placement by incoming buyers. Symmetric patterns are predicted for sellers’ choices.

In the previous models, asymmetric information is not allowed. Handa et al. (2003) extend Foucault’s (1999) model to allow for private information and a varying proportion of buyers and sellers. In this model, the thickness of the bid and ask sides of the LOB proxy for the proportion of high and low-valuation traders. Buy (sell) competition is expected to increase with the proportion of high (low) valuation traders, prolonging the expected time-to-execution of limit buy (sell) orders and thus making more attractive the use of buy (sell) market orders.

Regarding empirical research, several papers have shown that limit (market) order traders enter in the market when liquidity is scarce (plentiful). Thus, Biais et al. (1995), Al-Suhaibani and Kryzanowski (2000), Beber and Caglio (2005), and Ellul et al. (2007), among others, find that limit order submissions inside the quotes occur more frequently when the spread widens, while market order submissions are more likely when the spread is tight. Consistently, Ranaldo (2004) and Hall and Hautsch (2007) show that order aggressiveness and trading intensity both decrease with the bid ask spread. Similarly, Ahn et al. (2001) show that when transitory volatility, due to a

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3 paucity of limit orders, arises from the ask (bid) side, investors submit more limit orders  
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5 to sell (buy) than market orders to sell (buy).  
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9 Quoted depth on both sides of the market has also been found to matter. Griffiths et  
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11 al. (2000) and Rinaldo (2004) find that traders become more aggressive when their own  
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13 (opposite) side of the book is thicker (thinner). Chakrabarty et al. (2006) conclude that  
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15 investors aimed to reduce the expected time-to-execution of their limit orders should  
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17 submit them when the depth on the own (opposite) side is smaller (greater). Likewise,  
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19 Ellul et al. (2007) document that when quoted depth is large traders are more likely to  
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21 “jump the queue” by submitting limit orders with prices improving existing quotes and  
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23 less likely to submit limit orders with prices equal or worse than current quotes.  
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25 Additionally, positive (negative) bid-ask depth imbalances may anticipate short-term  
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27 price increases (decreases), since they attract additional limit orders on the deep side  
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29 and additional market orders on the thin side, rising the imbalance.  
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35 Recent studies show that order choice is a more complex phenomenon than the  
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37 simple dichotomy of the uninformed patient trader who submits a limit order and  
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39 passively waits for execution and the impatient trader who submits a market order and  
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41 demands immediate execution. Beber and Caglio (2005) provide evidence that order  
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43 choice and its interaction with the state of the LOB vary in periods characterized by  
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45 higher probability of informed trading. Their findings suggest that informed traders may  
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47 act strategically during these periods, using passive limit orders to hide their  
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49 information. Hasbrouck and Saar (2007) evidence that over one-third of the limit orders  
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51 submitted in INET are cancelled within two seconds. These “fleeting” limit order  
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53 traders are not meant to be patient liquidity providers. Pardo and Pascual (2007) and De  
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55 Winnie and D’hondt (2007) both show that the detection of hidden volume at the best  
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57 quotes temporarily increases order aggressiveness on the opposite side of the market.  
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A related line of research suggests that the state of the LOB may have informational content. Seppi (1997), Harris (1998), Moinas (2004), and Kaniel and Liu (2006) provide conditions under which informed traders, usually modeled as impatient, may be willing to use limit orders. Bloomfield et al. (2005) and Anand et al. (2005) provide experimental and empirical evidence supporting these last models' predictions. More recently, Foucault et al. (2006) develop a model in which limit order traders possess private information on the occurrence of future information events ("volatility information"), such as corporate announcements, and they adjust their order submissions to the level of risk perceived. Pascual and Veredas (2006) provide supporting evidence.

**3. Methodological details**

*3.1. The two-stage sequential ordered probit model*

As previously indicated, we understand order choice as a two stage process. In the first stage, the trader is characterized as patient or impatient, as she must choose between removing, providing, and consuming liquidity. The degree of patience of the incoming trader may be partially exogenous, but we allow it to be shaped by the state of different pieces of LOB information. In the second stage, the patient or impatient trader chooses among the different type of orders available according to their needs. This second step decision is essentially determined by the transient market conditions that, in the end, are nested in the state of the LOB.

An appropriate econometric model to analyze the sequential decision process described above is the Sequential Ordered Probit (henceforth SOP) model. In the first stage of the process, the degree of impatience of a given trader  $i$  arriving at the market is

a (linear) function of  $K$  observed variables,  $X_k$ ,  $k = 1, \dots, K$ . The aggressiveness index  $A_i^*$  is represented as

$$A_i^* = \sum_{k=1}^K \beta_k^A X_{ik}^A + \varepsilon_i^A = Z_i^A + \varepsilon_i^A, \quad [1]$$

where  $\varepsilon_i$  is the error term and  $\beta_k^A$  is the slope coefficient associated with the  $k^{\text{th}}$  regressor (to be defined later). Since  $A_i^*$  is difficult (if not impossible) to observe, equation [1] is a latent regression. However, it is possible to infer about the degree of the traders' impatience by observing the specific orders submitted. Thus, the three categories of order aggressiveness considered in this first stage (liquidity withdrawal, liquidity provision, and liquidity consumption) represent a partition of the state space that allows mapping the latent variable into observable discrete values. Let  $A_i$  be an ordinal response variable such that

$$A_i = \begin{cases} 1 & \text{if } A_i^* \leq \delta_1^A \\ 2 & \text{if } \delta_1^A < A_i^* \leq \delta_2^A, \\ 3 & \text{if } A_i^* > \delta_2^A \end{cases} \quad [2]$$

with  $\delta_1^A$  and  $\delta_2^A$  being unknown thresholds, to be estimated along with the slope parameters.  $A_i = 1$  means that the trader decides to leave the market and, accordingly, she withdraws liquidity by submitting a cancellation;  $A_i = 2$  means the trader is willing to assume certain degree of non-execution risk and, consequently, she will latterly provide liquidity by submitting a limit order; finally,  $A_i = 3$  means the trader is impatient and requires an immediate execution of their trading interests; at the end, she will therefore choose among the different types of market orders.

The probability that the incoming trader is of type  $j$  is

$$P_{ij}^A = P(\delta_{j-1}^A < A_i^* < \delta_j^A) = P(\delta_j^A - Z_i^A) - P(\delta_{j-1}^A - Z_i^A), \quad [3]$$

with  $\delta_0^A = -\infty$  and  $\delta_3^A = +\infty$ . Assuming that the probability distribution of the error terms  $\varepsilon_i$  is normal,  $\Pr(\delta_j^A - Z_i^A) = \Phi(\delta_j^A - Z_i^A)$ , where  $\Phi(\cdot)$  is the normal cumulative distribution function.<sup>5</sup> The corresponding log-likelihood is

$$\ln L^A = \sum_{i=1}^n \sum_{j=1}^3 d_{ij}^A \ln P_{ij}^A, \quad [4]$$

where  $d_{ij}^A = 1$  if  $A_i = j$  and  $d_{ij}^A = 0$  otherwise, maximized with respect to  $\beta_k^A$ ,  $\delta_1^A$  and  $\delta_2^A$ .

In the second stage of the SOP model, we analyze order choice by patient and impatient traders separately. Suppose, for instance, that trader  $i$  is patient.<sup>6</sup> The ordinal response variable  $L_i$  takes three possible values, given by the unobservable thresholds  $\delta_1^L$  and  $\delta_2^L$ ,

$$L_i = \begin{cases} 1 & \text{if } L_i^* \leq \delta_1^L \\ 2 & \text{if } \delta_1^L < L_i^* \leq \delta_2^L, \\ 3 & \text{if } L_i^* > \delta_2^L \end{cases}$$

where  $L_i^*$  represents the latent aggressiveness of the limit order trader,

$$L_i^* = \sum_{k=1}^K \beta_k^L X_{ik}^L + \varepsilon_i^L = Z_i^L + \varepsilon_i^L.$$

Whenever  $L_i^* \leq \delta_1^L$  the trader submits a non-aggressive limit order to buy (sell) below (above) the best bid (ask), and  $L_i = 1$ ; whenever  $\delta_1^L < L_i^* \leq \delta_2^L$ , the trader submits a limit

<sup>5</sup> If we assume a logistic distribution, equations [1] and [2] will define an ordered *logit* model. Preliminary estimations provide identical results under either assumption. Since related studies such as Griffiths et al. (2000) and Rinaldo (2004) assume normality, we also base our analysis on the ordered probit model.

<sup>6</sup> The following discussion is equivalent for an impatient trader that has to choose between three types of market orders, from lower to higher aggressiveness: a non-aggressive market order, a market-to-limit order, and an aggressive market order. In terms of notation, we would replace  $L$  by  $M$ .

order to buy (sell) at the current best bid (ask), and  $L_i = 2$ ; if  $L_i^* > \delta_2^L$ , the trader seeks a short time-to-execution and submits a limit order inside the best quotes, and  $L_i = 3$ .

The probability that an incoming trader submits a, say, limit order at the quotes is  $P_{i2}^A P_{i2}^L$  where  $P_{i2}^A$  is the probability of a patient trader arriving at the first stage ( $A_i = 2$ ) and  $P_{i2}^L$  is the unconditional probability of the patient trader submitting a limit order at the quotes ( $L_i = 2$ ) at the second stage. Let  $d_{il}^L = 1$  if  $L_i = l$  and  $d_{il}^L = 0$  otherwise, for  $l = 1, 2, 3$ . Because  $P_{i2}^A$  does not depend on  $l$  and  $\sum_{l=1}^3 d_{il}^L = 1$ , the log-likelihood of the second stage for the patient traders is

$$\ln L^L = \sum_{i=1}^n \ln P_{i2}^A + \sum_{i=1}^n \sum_{l=1}^3 d_{il}^L P_{il}^L, \quad [5]$$

The first term on the RHS of [5] does not play any role in the maximization of the log-likelihood, since the latter is maximized with respect to the parameters on the second RHS term ( $\beta_k^L$ ,  $\delta_1^L$  and  $\delta_2^L$ ).

The SOP approach is conceptually different to the OP approach. The latter presumes that any trader arriving at the market, independently of their degree of patience, chooses among all the possible type of orders. That is,

$$O_i = \begin{cases} 1 & \text{if } O_i^* \leq \delta_1^O \\ 2 & \text{if } \delta_1^O < O_i^* \leq \delta_2^O, \\ \vdots & \\ 7 & \text{if } O_i^* > \delta_7^O \end{cases}$$

where  $O_i^* = \sum_{k=1}^K \beta_k X_{ik} + \varepsilon_i^O = Z_i + \varepsilon_i^O$  and  $P_{ik}^O = \Pr(O_i = k) = \Phi(\delta_k^O - Z_i) - \Phi(\delta_{k-1}^O - Z_i)$ .

In this case,  $O_i = 1$  is a cancellation,  $O_i = 2$  is a non-aggressive limit orders, and so on and so forth. In contrast to the SOP model, an increase in  $X_{ik}$ , for example, the bid-ask



spread, will be predicted to affect in exactly the same manner to all types of traders through a single parameter. With the SOP model however, an increase in the bid-ask spread may affect differently the order choice of patient and impatient traders through one parameter for the first stage and two parameters for the second stage.

The extra computational demand of the SOP model is marginal since the optimization of the SOP model boils down to the optimization of two OP models. Nonetheless, the OP and the SOP models are not nested because the estimated probabilities of observing the different events in the second stage and, hence, the likelihood function, depend on the probabilities of the first stage, as shown in equation [5].

A general drawback of all these models is that, given a change in a regressor, it is only the direction of change in the probabilities of the two extreme cases that can be unambiguously determined from the sign of the associated coefficient.<sup>7</sup> The more levels or categories, the more limited the model. Thus, in an OP model with seven levels of aggressiveness, as that suggested in previous studies, the sign of the coefficients may fail to describe the direction of change in the probabilities of the five intermediate categories. This problem is significantly lessened with the SOP model since each node in the decision process involves only three possible outcomes and, thus, only one category is left in each stage with an ambiguous probability change. We compute marginal probabilities to clarify the direction of the change in probabilities. They measure the expected increase in the probability of each category after a marginal increase in a given regressor. In the first stage, the marginal effect of, say, the  $k$ th regressor on the probability of  $A_i$  taking value  $m$  is,

<sup>7</sup> See Borooah (2001, p. 23-24) and Greene (2003, p. 738-739) for further details on this issue.

$$\frac{\partial P(A_i = m)}{\partial X_{ik}^A} = \begin{cases} -\phi(\delta_1^A - Z_i^A) \beta_k^A & \text{if } m = 1 \\ [\phi(\delta_1^A - Z_i^A) - \phi(\delta_2^A - Z_i^A)] \beta_k^A & \text{if } m = 2 \\ \phi(\delta_2^A - Z_i^A) \beta_k^A & \text{if } m = 3 \end{cases} \quad [6]$$

where  $\phi(\cdot)$  is the normal density function. For the second stage, marginal probabilities are defined analogously.

### 3.2. Order aggressiveness

We use a generally accepted categorization of order aggressiveness originally proposed by Biais et al. (1995) that has been used, with some minimum variations, in previous papers. From the most to the least aggressive category,

- C7: Buy (sell) orders that demand more volume than is available at the best prevailing ask (bid) and are allowed to walk up (down) the book.
- C6: Buy (sell) orders that demand more volume than is available at the best ask (bid) but are not allowed to walk up (down) the book.
- C5: Buy (sell) orders that demand less volume than is available at the best ask (bid).
- C4: Orders with prices lying between the best bid and offer.
- C3: Buy (sell) orders with prices equal to the best bid (ask).
- C2: Buy (sell) orders with prices below (above) the best bid (ask).
- C1: Cancellations.

Categories C5 to C7 imply total or partial immediate execution of the order and, therefore, consume liquidity. These are the possible choices we consider for an impatient trader in the second stage of the SOP model. Categories C2 to C4 imply non-immediate execution and, therefore, provide liquidity. These are the possible choices we

consider for a patient trader in the second stage of the SOP model. Category C1 includes orders that withdraw liquidity, and they are to be chosen exclusively in the first stage of the SOP model.

3.3. *Pieces of LOB information*

We consider two large pieces of LOB information. The *best quotes* (henceforth *BQ*) set includes the following variables, all of them defined with respect to the incoming order:

- *SPR*: Bid-ask spread.
- $NS^l$  ( $NO^l$ ): Pending number of orders on the same (opposite) side of the book.<sup>8</sup>

The *additional quotes* (hereafter *AQ*) set includes,

- $NS^{25}$  ( $NO^{25}$ ): Accumulated number of orders on the same (opposite) side of the book.
- $LS^{l2}$  ( $LS^{25}$ ): Distance, in ticks, between the best and the second best (the second best and fifth best) quotes on the same side of the book.
- $LO^{l2}$  ( $LO^{25}$ ): Distance between the best and the second best (the second best and fifth best) quotes on the opposite side of the book.

The information contained in the second set of variables could be thought of as consisting of two components: Redundant information already contained in the best quotes, and brand new information only present in the secondary levels. To isolate the latter piece of information, the *AQ* set is defined as the residuals of a linear regression of each of its components on the contemporaneous and lagged values of the variables in

<sup>8</sup> We also considered the quoted depth as an alternative to the number of orders. The correlation between both proxies was very high, so that our main findings barely differed. In this final version, we only report the analysis based on the number of orders.

the  $BQ$  set. In this way, any explanatory power attributed to the secondary levels of the book will be (linearly) unconnected with the information on the best quotes.

We consider three alternative specifications for the SOP model. The “Baseline” model (BM) only includes the first lag of the dependent variable in the explanatory variable set; the “Best Quotes” model (BQM) adds the  $BQ$  set of explanatory variables to the BM model; the “Complete Book” model (CBM) adds the  $AQ$  set of explanatory variables to the BQM. In the next sections, we will evaluate the relative performance of each specification in each stage of the SOP model both in-sample and out-of-sample. We will also compare the performance of the CBM-SOP model with an alternative CBM-OP model.

### 3.4. Hypotheses

The choice of LOB variables described above is supported by the existing literature. According to Foucault (1999), Foucault et al. (2005), and Rinaldo (2004), we hypothesize that the wider the spread, the higher the frequency of patient traders on the first stage of the SOP model. A wider spread increases the costs of trading aggressively. In the second stage, we expect a lower proportion of the least aggressive market orders (C5) in favor of most aggressive (C7) market orders as the inside spread increases. This hypothesis builds on the fact that C7 traders bear higher immediacy costs than those given by the inside spread, since they consume more than the depth available at the best opposite quote. Contrarily, immediacy costs of C5 orders are entirely determined by the spread. We therefore expect C5 orders to be more sensible than C7 orders to variations in the inside spread. Regarding limit orders, according to Foucault (1999), Foucault et al. (2005), and Goettler et al. (2005) we should expect limit order traders to become more aggressive in their price improvements as the bid-ask spread widens. Therefore,

we hypothesize limit order traders to submit more C4 (inside the best quotes) limit orders as the spread increases.

Regarding quoted depth at the best quotes, the crowding out effect of limit orders predicted by Parlour (1998) sets the basis for our hypotheses. Additionally, in Handa et al.'s (2003) framework higher imbalances between buyers and sellers are to be associated with increased order aggressiveness. Ranaldo (2004), Ahn et al. (2001), and Ellul et al. (2007), among others, provide supporting empirical evidence. Accordingly, in the first stage of our SOP model, we expect an increase in the rate of arrival of impatient (patient) buyers (sellers) when the quoted depth at the best bid quote increases. Similarly, increases in the depth at the best ask is expected to encourage more impatient (patient) sellers (buyers).

With respect to limit order traders in the second stage, a larger depth at the best quote makes it more attractive to “jump the queue” by submitting inside the quote (C4) limit orders and conversely less attractive to submit limit orders at the quote (C3) or away from the best quote (e.g., Ellul et al., 2007). Traders with stale limit orders may also engage in a “chasing” strategy (see Hasbrouck and Saar, 2007) consisting of canceling the old limit orders and resubmitting them more aggressively. Moreover, according to Parlour (1998), we expect patient traders on the thinner side of the market to submit less aggressive limit orders, anticipating an increase in the arrival rate of market orders from the opposite side.

Coppejans et al. (2004) provide evidence that the actual costs incurred by traders are significantly lower than the costs that would be incurred under a raw strategy that would ignore time-variations in liquidity, particularly for large trades. They conclude that traders act strategically, taking advantage of periods of liquidity surpluses and avoiding liquidity deficits. Their finding also agrees with traders fitting order size to the state of

the LOB, for example, by splitting orders into smaller (C2) ones, or by submitting market-to-limit (C3) orders. Thus, in Mendelson and Tunca (2000), discretionary liquidity traders adjust the order size along with the changing market depth, equalizing trading costs across sizes. Similarly, De Winnie and D'hondt (2007) and Pardo and Pascual (2007) both show that the detection of hidden volume on the best opposite quote fosters order aggressiveness. Traders behave strategically, however, and just seize the opportunity for depth improvement, without consuming more than available at the best opposite quote. In accordance with the previous findings, we would expect the available depth at the best quotes of the LOB to shape the size of the incoming market orders, but we would not expect an increase in the proportion of aggressive market orders. Namely, we hypothesize an increase in the submission of C5 market orders in the second stage of our SOP model as  $NO^I$  goes deeper.

Goettler et al.'s (2005) model predicts that a deep book away from the best ask (bid) quote signals that the best quote price is "too low" ("too high"). Their simulation results suggest that the higher  $NS^{25}$ , the lower the frequency of both market orders and aggressive limit orders, and the higher the frequency of limit orders at or away from the best quote. Contrarily, higher  $NO^{25}$  may lead to more aggressive order submissions. Accordingly, we hypothesize  $NS^{25}$  ( $NO^{25}$ ) to decrease (increase) the aggressiveness of both patient and impatient traders order choices in the second stage of the SOP model. Regarding the first stage of the SOP model, our prediction is more ambiguous. Order imbalances beyond the best quotes may reinforce Parlour's (1998) crowding out effect. Thus, increased competition in the form of depth below (above) the best bid (ask) may result in a higher frequency of impatient (patient) buyers (sellers). Deep book imbalances may also anticipate short-term price movements, as suggested by Kavajecz and Odders-White (2004). Since rising (falling) markets are expected to prolong

(shorten) the time-to-execution of limit buy (sell) orders, a thick bid (ask) book beyond the best quotes may induce incoming buyers (sellers) to be more impatient and incoming sellers (buyers) to be more patient.<sup>9</sup> The simulations in Goettler et al. (2005), however, point towards the opposite prediction (see Tables IV and VI in p. 2170). We therefore treat the impact of  $NS^{25}$  and  $NO^{25}$  on the first stage of the SOP model as a theory-free empirical issue.

“Length” measures are less common in microstructure research. Given the quoted depth, the length of the LOB determines the expected price impact of large market orders. Thus,  $LO^{l2}$  measures the demanded compensation for consuming more than available at the best opposite quote. According to Glosten (1994), a lengthy ask (bid) book may indicate that potential sellers (buyers) have higher upper (lower) tail expectations. As long as this signaling effect outweighs the increased costs of trading, a lengthy ask (bid) book may increase buy (sell) pressure (see Hall and Hautsch, 2007). Similarly, a lengthy book on the ask side may suppose a longer time-to-execution for a limit buy order, causing incoming buyers to be more aggressive and, consequently, reducing the waiting costs of incoming patient sellers. Following this reasoning, we expect the length of the book to reinforce the crowding out effect on the first stage of the SOP model: the length of the ask (bid) side is expected to be positively correlated with the frequency of impatient buyers (sellers) and positively correlated with the probability of patient sellers (buyers). Regarding the second stage, all else equal, we would expect a high  $LO^{l2}$  to discourage the most aggressive type of market order (C7) traders because of the increased costs of transaction. A narrow  $LS^{l2}$  may signal a crowded LOB, which may encourage patient traders to place their orders in front of the queue so as to gain time precedence. In line with Glosten (1994), we would also expect

<sup>9</sup> Beber and Caglio (2005) and Chan (2005) report a positive connection between momentum and order aggressiveness.



high values of  $LS^{l2}$  and  $LS^{25}$  to discourage aggressive limit order submissions since they may signal a high perceived picking-off risk.

#### 4. Market background and data

The Spanish Stock Exchange Interconnection System (henceforth SIBE) is the electronic platform that, since 1995, holds all the Spanish stocks that achieve pre-determined minimum levels of trading frequency and liquidity.<sup>10</sup> Every order submitted to the system is electronically routed to a centralized LOB.

The SIBE is organized as an order-driven market with a daily continuous trading session, from 9:00 a.m. to 5:30 p.m., and two call auctions that determine the opening and closing prices. During the continuous trading session, a trade takes place if and only if an order hits the quotes. Pre-arranged trades are not allowed, and price-improvements are impossible.<sup>11</sup> There are no market makers, and there is no floor trading. The market is governed by a strict price-time priority rule. The minimum price variation (tick) equals €0.01 for prices below €50 and €0.05 for prices above €50. The minimum trade size is one share.

There are three basic types of orders: market, limit, and market-to-limit. Market orders execute against the best prices on the opposite side of the LOB. Any excess that cannot be executed at the best bid (ask) quote is executed at less favorable prices by walking down (up) the book until the order is fulfilled. Market-to-limit orders are limited to the best opposite-side quote at the time of entry. Any excess that cannot be executed is converted into a limit order. Finally, limit orders are to be executed at the

<sup>10</sup> According to the Focus Monthly Bulletin of June 2006 of the World Federation of Exchanges ([www.world-exchanges.org](http://www.world-exchanges.org)), the Spanish market is the fourth European market in terms of market capitalization (\$US 1,116,146 millions), right after the LSE (\$US 3,370,070 millions), Euronext (\$US 3,192,428 millions) and the Deutsche Bourse (\$US 1,412,118 millions). The SSE is also the 4<sup>th</sup> European market in terms of total value of share trading.

<sup>11</sup> Because of the allowance of hidden limit orders, however, depth improvements are possible.



limit price or better. Any unexecuted part of the order is stored in front of the book at the limit price. Market orders belong to the C5 to C7 categories of aggressiveness previously defined, market-to-limit orders are C6 orders, and limit orders are C2 to C4 orders.<sup>12</sup> By default, all orders expire at the end of the session.<sup>13</sup>

Our database consists of all the updates of the 5 best bid/ask quotes of the LOB and all trades executed from July to December 2000 (124 trading days) during the continuous trading session. The LOB data includes quotes, disclosed depth, and the number of orders supporting each quote. All the movements of the book are time-stamped to the nearest hundredth of a second. The trading data is updated each time the best quotes change. It details the trade price, the trade size, and the best quotes before and after each trade. We match both files using an algorithm introduced by Pardo and Pascual (2007). Once matched, we can classify all the LOB updates into one of the seven categories of aggressiveness formerly defined. It is also easy to distinguish

<sup>12</sup> Limit orders at a price equal to the best quote on the opposite side of the book and of smaller (larger) size than the quantity available at that opposite quote cannot be distinguished in practice from market (market to limit) orders. Therefore, we pool them as C5-market (C6-market to limit) orders. Similarly, we put together limit orders that walk up or down the book and become totally fulfilled with C7-market orders, and market-to-limit orders with size smaller than the available depth as C5-market orders. Limit orders that walk up or down the book but are only partially executed represent less than 0.3% of all orders submitted. These orders are also considered C7. By a limit order that walks up or down the book we mean a limit order to buy (sell) which price is above (below) the prevailing best ask (bid) quote and which size is larger than the depth available at the best opposite quote. This order will consume the best ask (bid) quote on the book, and the excess will be executed at less favorable ask (bid) prices until it either fully executes or reaches a quote above (below) the limit price.

<sup>13</sup> For all type of orders, brokers may specify special conditions: (a) “Execute or eliminate” means the order must be executed immediately. In case of partial execution, the unexecuted part must be eliminated right away. (b) “Fill or kill” also requires instantaneous execution. In this case, partial execution is not possible. The order must be fully executed or fully eliminated. (c) “Minimum execution” implies that at least a given part of the order must be immediately executed. If the minimum execution is not possible, the whole order must be eliminated. If the minimum execution is possible, the rest of the order must be treated as a regular order. (d) Finally, partially undisclosed limit orders, known as “iceberg” orders, are allowed. Our database does not identify orders submitted with special conditions. Hidden orders, for example, are only detectable upon execution. In practical terms, orders with these conditions are therefore undistinguishable from some of the seven categories of aggressiveness defined above. In this paper, we consider the undisclosed depth when classifying orders. We classify all orders relative to the total depth (disclosed plus undisclosed) available at the best quotes. Market orders with size larger than the disclosed depth at the best-opposite quote on the book are classified as C7 if and only if they exhaust all the available depth at that quote.

between buyer and seller initiated trades because the LOB always acts as the passive side on every trade.

The SSE database has some drawbacks we consider convenient to mention. We observe pictures of the whole book, but we do not have information order by order. Therefore, we cannot follow the history of all the orders submitted. This is a limitation because we can not compute the realized time-to-execution or time-to-cancellation of all limit orders. We do not have LOB information about the opening and closing auctions. We must therefore exclude these relevant periods for price discovery from our analysis. The initial LOB each day, however, corresponds to the unexecuted limit orders coming from the pre-auction phase. So, the role these orders play in order choice is considered. Moreover, the SSE allows submitting iceberg orders. Recent empirical studies (see De Winnie and D'hondt, 2007, and Pardo and Pascual, 2007) have shown that the state of the LOB matters in choosing between disclosed and undisclosed limit orders. Moreover, hidden volume, when revealed to the marketplace, affects order choice by increasing order aggressiveness on the opposite side of the market. It would be therefore desirable to extend our analysis by including iceberg orders either as an additional possible order choice by incoming traders or as a conditional variable for order choice. Unfortunately, we can only detect the presence of iceberg orders at execution and, even then, we cannot always know the exact amount of the hidden volume. Thus, we leave this possible extension for future research.

Our initial sample consists of all the stocks that were part of the official market index, the IBEX-35, during 2000.<sup>14</sup> We exclude one stock involved in a merger. Table I provides descriptive statistics on the 36 stocks conforming the final sample. It is

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<sup>14</sup> The IBEX-35 is composed of the 35 most liquid and active SIBE-listed stocks during the most recent six-month control period. The composition is ordinarily revised twice a year. Extraordinary revisions are possible due to major events like mergers or new stock issues. During 2000, a total of 37 stocks were index constituents.

possible to appreciate huge differences between them in terms of both liquidity and activity. The most illiquid stock in the sample (ALB) shows a bid-ask spread which is 14.2 times larger (in number of ticks) than the most liquid stock (SCH), a quoted depth at the ask side (in number of shares) which is 60.5 times smaller, and a distance between the first and the fifth ask quotes in the book, also in number of ticks, which is 5 times larger. Similarly, the most active stock (TEF) presents an average daily volume (in shares) and an average daily number of trades which are, respectively, 157 and 86.7 times larger than the corresponding statistics for the least frequently traded stocks (ANA and AUM). Our sample is representative in the sense that it represents about 94% of the total volume traded and 64% of the total market capitalization.

[Table I]

In the next section, we evaluate the relative performance of each SOP model in section 3, both in-sample and out-of-sample. For in-sample analyses, we use data from July to November 2000. For out-of-sample analyses, we use December 2000 data.

5. Empirical findings

Table II provides summary statistics about order aggressiveness. We classify each update of the LOB into the 7 categories of aggressiveness defined earlier. We provide the distribution of orders by category over all the orders submitted (Panel A) and over buyer-initiated and seller-initiated orders (Panel B). The most frequent category is small market orders (C5), which represents 40.39% of all orders submitted. The least frequent category is that of large market orders (C7), which represent 3.75% of all orders.<sup>15</sup> According to Panel A, 35.39% of the orders submitted provide liquidity, 50.21% consume liquidity, and 14.41% withdraw liquidity. We do not find remarkable

<sup>15</sup> Similar patterns are reported by Rinaldo (2004), for the Swiss Stock Exchange, Griffiths et al (2000) for the Toronto Stock Exchange, Biais et al (1995) for the Paris Bourse, now Euronext, Al-Suhaibani and Kryzanowski (2000) for the Saudi Stock Market, and Beber and Caglio (2005) for the NYSE.

differences between buyer-initiated and seller-initiated orders. Even though our sample period is biased by a bear phase, the IBEX constituents, for the most part, remained relatively stable.

[Table II]

Table III summarizes the maximum likelihood estimation of the first stage of the CBM SOP model for the 36 stocks. We estimate separated models for buyer-initiated traders and seller-initiated traders. We also provide the marginal probabilities in [6] evaluated at the mean of the explanatory variables.

[Table III]

We find a strong first order positive autocorrelation in order aggressiveness. That is, the probability of observing an aggressive type of order increases if the immediately preceding event on the same side of the market is also an aggressive order. This is consistent with the “diagonal effect” reported by Biais et al. (1995), but it is at odds with Parlour (1998), who predicts that submitting an aggressive order is less attractive when the immediately preceding order at the same side is a limit order. Similar order-by-order serial correlation in order type is provided by Ellul et al. (2007).<sup>16</sup>

The estimated coefficients for the  $BQ$  set are consistent with previous empirical findings (using the OP model), and corroborate the hypotheses posted in section 3. A wider spread increases the probability of the incoming trader being patient, consistently with Foucault (1999), a finding supported by almost all the stocks in our sample. Consistent with Parlour’s (1998) crowding out effect, we find that the thicker the book on the buy (sell) side, the more impatient the incoming buyer (seller) becomes. Marginal probabilities show that, as the bid-ask spread (depth at the own side) increases

<sup>16</sup> Biais et al. (1995) argue that this diagonal effect may reflect imitative behavior by uninformed traders, order splitting, traders reacting to the same public information, or competition between liquidity providers.

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2  
3 the probability of the most impatient type of trader decreases (increases), while the  
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5 probability of the most patient types increases (decreases).  
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9 Regarding depth at the best opposite quote, we find a statistically significant and  
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11 negative relationship, consistent with Parlour’s (1998) prediction that a thicker book on  
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13 the sell (buy) side will decrease the impatience of new buyers (sellers). Marginal  
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15 probabilities, however, show that sellers’ behavior is at odds with them expecting a  
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17 crowding out effect. This finding might be a result of the bear market affecting our  
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19 sample period. However, Beber and Caglio (2005) report the same asymmetry for the  
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21 NYSE using the TORQ database. They argue this finding indicates that sellers are more  
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23 impatient than buyers, and prefer to take advantage of the lower costs of liquidity. In  
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25 any case, the marginal probabilities show that  $SPR$  and the  $NS^l$  have a major impact,  
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27 with  $NO^l$  being less relevant.  
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33 Regarding the  $AQ$  set, Table III shows these variables are less important than the best  
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35 quotes in characterizing incoming traders’ patience. For secondary depth ( $NO^{25}$  and  
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37  $NS^{25}$ ), our findings support the hypothesis that the book beyond the best quotes may  
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39 reinforce the crowding out effect predicted by Parlour (1998). In addition, the marginal  
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41 probabilities confirm that, in this case, the finding is consistent among sellers and  
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43 buyers. Therefore, in our sample, the crowding out effect for sellers is fully satisfied  
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45 when we consider the secondary book depth. We also obtain a weak negative effect of  
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47  $LS^{l2}$  and a strong positive effect of  $LO^{l2}$  on order aggressiveness. As previously  
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49 discussed, a small  $LS^{l2}$  may signal a crowded book on the same side of the market as the  
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51 incoming trader. This variable therefore reinforces the findings obtained with  $NS^l$  and  
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53  $NS^{25}$ . Moreover, a rational buyer (seller) will interpret a higher dispersion on the ask  
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55 (bid) side of the book as a longer expected time-to-execution for a new limit order to  
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57 buy (sell), inducing the incoming buyer (seller) to be more aggressive. Finally, both  
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$LS^{25}$  and  $LO^{25}$  tend to decrease the frequency of aggressive traders. In terms of statistical significance, however, this last relationship is weak.

Table IV shows, for the first stage of the SOP model, the relative in-sample and out-of-sample performance of each of the three model specifications (BM, BQM and CBM). We report four alternative goodness-of-fit measures that correspond to the in-sample (adjusted) pseudo- $R^2$ s of McFadden (1973, p.121), Maddala (1983, p.39) with the Cragg and Uhler (1970) correction, Aldrich and Nelson (1984) with the Veall and Zimmermann (1992) correction, and McKelvey and Zavoina (1975).<sup>17</sup> For each measure, we provide its median across the 36 stocks for the BM, its percentage increase for the BQM with respect to the BM, and for the CBM with respect to the BQM.

[Table IV]

The results across measures are similar. Consider the McKelvey and Zavoina's pseudo- $R^2$ . When the  $BQ$  variables are added to the simplest autoregressive model, we get an in-sample fit improvement of 51.68% for sellers and 82.75% for buyers. In addition, when the whole LOB is taken into account the fit improves an additional 52.40% for sellers and 42.57% for buyers. This increasing pattern indicates that the state of the book determines, at least partially, the nature of the incoming trader. Moreover, traders examine not only the best quotes, but also the less aggressive quotes. Our results seem to attribute a more noteworthy role to the book beyond the best quotes than it should be expected given Cao *et al*'s (2003) findings. Similarly, from the out-of-

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<sup>17</sup> No one of these measures is universally accepted or employed. The values between zero and one have no natural interpretation, though it has been suggested that the pseudo- $R^2$  value increases as the fit of the model improves. In a comparative analysis performed by Veall and Zimmermann (1996), these authors conclude that, for the particular case of the ordered probit model, the pseudo- $R^2$  due to McKelvey-Zavoina outperforms the other measures and has a strong numerical relationship to the OLS- $R^2$  in the latent variable. The Veall-Zimmermann and the Cragg-Uhler's measures also perform reasonably well. We include the McFadden's pseudo- $R^2$  because it is the most common in statistical packages. For a review of all these goodness-of-fit measures see Veall and Zimmermann (1996). As in standard regression analysis, we use adjusted versions of these measures to take into account the inclusion of additional explanatory variables.

sample McKelvey-Zavoina (adjusted) pseudo- $R^2$ , we observe that the predictive capacity of the BQM outperforms that of the BM by a median 108.96% for sellers and 141.22% for buyers. When the complete book is considered there is an additional improvement of 31.39% for sellers and 40.11% for buyers.

As an alternative to the previous point measures of goodness-of-fit, we perform the following forecasting exercise. Using the in-sample estimated coefficients, we compute the one-step-ahead forecasting probability for each of the 3 categories of aggressiveness and for each out-of-sample observation. Then, we compute how often the SOP model beats the unconditional probability given by the in-sample relative frequency of each category. The results are summarized at the bottom panel of Table IV. We find that the CBM outperforms the BQM and the BM. The CBM beats the unconditional frequency more often than the other two models for 47.22% for both buyers and sellers; only for 22.22% (16.67%) of the stocks the BQM outperforms the other two models for sellers (buyers). We also provide a direct comparison between models. The CBM does better than the BQM for 94.44% (97.22%) of the stocks in sellers (buyers) model, in the sense that the CBM allocates a higher probability to the actual category of aggressiveness than the BQM. Both book models usually improve on the BM.

Table V summarizes the estimation of the second stage of the CBM. We report the coefficients for patient (Panel A) and impatient (Panel B) traders, distinguishing between buyer and seller-initiated orders, in separated panels. We also provide the marginal probabilities in each case.

[Table V]

Table V provides evidence that the bid-ask spread is very important in determining both patient and impatient order choices. Marginal probabilities in Panel A show that



patient traders submit more aggressive limit orders (C4) as the bid-ask spread increases. This finding is consistent with the theoretical predictions of Foucault et al. (2005), with previous empirical evidence (e.g., Biais et al., 1995, and Ranaldo, 2004), and with our hypothesis in section 3. Regarding impatient traders, marginal probabilities in Panel B report a strong decrease in the likelihood of submitting C5 orders, which favors an increase in the proportion of C6 and C7 orders. This finding provides support to our hypothesis in section 3 that an increase in the inside spread has more dramatic consequences on the least aggressive type of traders among all the impatient ones.

Regarding quoted depth at the best quotes, Table V shows that same-side (opposite-side) depth is more relevant for patient traders' (impatient traders') order choices. Marginal probabilities in Panel A show that patient traders facing a thick best quote (a large  $NS^I$ ) are more likely to "jump the queue", which is consistent with Handa et al.'s (2003) arguments, among others. As hypothesized, the submission of inside-the-quotes (C4) limit orders increases as  $NS^I$  augments, in detriment of less aggressive types (C3 and C2) of limit orders. Contrarily,  $NO^I$  is only statistically significant for 3 (2) stocks for patient buyers (sellers).

Even though a deep best bid (ask) increases the rate of arrival of impatient buyers (sellers) (see Table III), the marginal probabilities in Panel B indicate that these additional traders use to submit C5 (non-aggressive) market orders. This last finding is weak, anyway:  $NS^I$  is only statistically significant for 14 (10) stocks for impatient sellers (buyers). Quite the opposite, the thickness of the best opposite quote has a strong effect on order choice by impatient traders. As hypothesized in section 3, the higher the  $NO^I$ , the higher (lower) the proportion of impatient traders choosing C5 (C6 and C7) market orders. This behavior is observed for both buyers and sellers, despite the asymmetric pattern evidenced in the first step of the SOP model. Thus, impatient traders



1  
2  
3 take advantage of liquidity surpluses and adjust the size of their orders to the available  
4  
5 opposite depth, probably seeking to equalize the trading costs across trade sizes, as in  
6  
7 Mendelson and Tunca (2000).  
8  
9

10  
11 Albeit the  $BQ$  set is much more relevant, the  $AQ$  set also determines order choice at  
12  
13 the second stage of the SOP model. Panel A in Table V shows that patient buyers'  
14  
15 (sellers') order choices depend more on the book beyond the best bid (ask) than on the  
16  
17 book beyond the best ask (bid). Among all the  $AQ$  variables,  $LS^{l2}$  is found to be the  
18  
19 most relevant. In general, the length of their own side of the book decreases the  
20  
21 aggressiveness of incoming limit order traders. As with  $NS^l$ , a narrow  $LS^{l2}$  may signal a  
22  
23 crowded LOB (or a low picking-off risk), which encourages patient traders to place  
24  
25 their orders in front of the queue so as to gain time precedence. We also find  $NS^{25}$  to be  
26  
27 negatively related to the aggressiveness of patient traders, which is totally consistent  
28  
29 with the simulation results in Goettler et al. (2005). A crowded book beyond the best  
30  
31 ask (bid) quote signals the best quote is too low (high) leading incoming patient traders  
32  
33 on the same side to be more conservative. As far as we know, this is the first paper  
34  
35 providing empirical support to Goettler et al.'s (2005) prediction. The remaining same-  
36  
37 side variables are less critical. The incidence of the opposite side of the book on the  
38  
39 aggressiveness of the incoming limit order trader, as given by  $NO^l$ ,  $LO^{l2}$  and  $LO^{25}$ , is  
40  
41 weak.  
42  
43  
44  
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48

49  
50 With regard to impatient traders, marginal probabilities in Panel B of Table V point  
51  
52 towards  $LO^{l2}$  as the most remarkable determinant of order choice in the  $AQ$  set. As  
53  
54 discussed in section 3, as  $LO^{l2}$  increases it becomes more attractive to submit non-  
55  
56 aggressive (C5) market orders, and less attractive to submit aggressive (C7) market  
57  
58 orders. We also find that  $NO^{25}$  is positively related to the aggressiveness of the  
59  
60 incoming impatient traders on the opposite side of the market, which is consistent with

Goettler et al.'s (2005) simulation results. Hence, C7 buy (sell) orders are more frequent when the LOB away from the best ask (bid) quote signals that the best ask (bid) is too low (high). Consistently, we also report a negative effect of  $NS^{25}$  (also  $LS^{12}$  and  $LS^{25}$ ) on the aggressiveness of the incoming impatient trader.

Table VI reports the relative in-sample and out-of-sample performance of the second stage of the three SOP models considered.

[Table VI]

The in-sample analysis shows that limit order traders' choices crucially depend on the book information. There is a median improvement 134.48% for sellers and 177.09% for buyers when the best quotes are taken into account. More important, the CBM improves on the BQM by a median of 263.19% for sellers and 210.51% for buyers, implying that patient traders take their decisions by examining not only the best quotes but also the book beyond the best quotes. The out-of-sample (adjusted) pseudo- $R^2$  leads to the same conclusion. In addition, the CBM obtains the best scores against the relative frequency rule. It always outperforms the BQM, allocating higher probabilities to the actual event than the BQM and the BM.

The results for the impatient traders are remarkably different. Table VI shows that impatient traders' order choices depend, to a great extent, on the best quotes. There is a median in-sample fit improvement of 1100% for sellers and 991% for buyers when the  $BQ$  set is added to the simplest model. However, the CBM improves on the BQM only by a median 23.75% for sellers and 34.03% for buyers. This finding suggests that the most impatient traders base their strategic decisions primarily on the best quotes. The out-of-sample predictive performances support this conclusion: the pseudo- $R^2$  for sellers (buyers), for example, increases a negligible 7.82% (21.88%) from the BQM to the

CBM. Moreover, book-based models rarely do better than the relative frequency rule and the BQM probabilities outperform those of the CBM as many times as the CBM outperforms the BQM.<sup>18</sup>

As a final empirical analysis, we compare the performance of the two-stage SOP model with the one-stage OP model. We repeat the forecasting exercise at the bottom of Tables IV and VI but comparing the CBM-SOP model with the CBM-OP model. This time, we perform the analysis both in-sample and out-of sample. Our findings are summarized in Table VII. We report the number of stocks and the percentage of observations for which the SOP model outperforms the OP model, in the sense that the former model attributes a higher probability to the actual event than the latter model. We find that the SOP model beats the OP model in-sample for 100% of the stocks and about 60% of the observations, both for buyer-initiated and seller-initiated orders. The out-of-sample analysis provides similar figures. When we control for the type of order, we find that the SOP model beats the OP model in almost all categories, both in-sample and out-of-sample, with the exception being cancellations in-sample. The improvement is particularly remarkable for the most aggressive categories.

[Table VII]

**6. Summary and conclusions**

We study the role the limit order book (LOB) plays in order choice by both patient and impatient traders. Our contribution is twofold. This is the first paper in modeling order aggressiveness using a two-stage sequential ordered probit (SOP) model. The

<sup>18</sup> We have also performed likelihood-ratio tests to compare the three model specifications. For all the stocks and for all the stages of the SOP model, the BQM model is found to beat the BM model, and the CBM to beat the BQM at the 1% level. Therefore, we corroborate that the book beyond the best quotes matters. Moreover, the chi-square values suggest that secondary levels of the book are more useful to explain patient traders' decisions than to impatient traders' decisions. These findings are available upon request from the authors.

SOP model allows studying patient traders' order choices and impatient traders' order choices separately. This is valuable because we are able to separate the decision of whether to withdraw, provide or consume liquidity, from the decision of choosing a particular type of order. We show the superior forecasting performance, both in-sample and out-of-sample, of the SOP model versus the traditional ordered probit model of order aggressiveness.

We also contribute to the literature by considering the whole LOB, instead of just the best quotes, in explaining order choice. We distinguish between two pieces of book information, the best quotes and the book beyond the best quotes. We evaluate the relative improvement on the in-sample and out-of-sample goodness-of-fit performance of the SOP model when different pieces of book information are sequentially added as regressors.

We find that the whole book contributes in determining whether a trader becomes a liquidity provider or a liquidity consumer, though the inside spread and the quoted depth at the best quote on the same side as the incoming trader are particularly powerful. Patient traders crucially rely on the book beyond the best quotes to place their limit orders. In contrast, impatient traders primarily depend on the best quotes. Our findings also qualify previous empirical studies:

- (a) The frequency of patient traders increases with the bid-ask spread, and decreases with the thickness of the depth at the best quote on the same side of the market. The thickness of the best quote on the opposite side of the market has an asymmetric impact. It increases the frequency of patient buyers while it increases the frequency of impatient sellers. The book beyond the best quotes reinforces Parlour's (1998) "crowding out" effect.

- (b) Consistently with Foucault et al. (1995), we find that the higher the bid-ask spread, the higher the frequency of inside-the-quotes limit orders. A wider spread also decreases the likelihood of non-aggressive market orders, increasing the frequency of the most aggressive type of market orders.
- (c) Patient traders base their order choices primarily on the state of the LOB on the same side of the market, while impatient traders mostly look at the state of the LOB on the opposite side. Patient traders submit more aggressive limit orders as the depth at the best quote increases, while their choice is almost unaffected by the opposite side depth at the best quote. Impatient traders submit less aggressive market orders as the thickness of the opposite quote increases. They take advantage of liquidity surpluses while adjusting the size of their orders to the available depth, as in Mendelson and Tunca (2000).
- (d) Consistently with Goettler et al. (2008), we show that a thicker LOB beyond the best ask (bid) signals that the best quote is too low (high). Thus, the deeper the book above (below) the best ask (bid), the more aggressive both patient and impatient buyers (sellers) become.
- (e) A lengthy book on the opposite (same) side of the market, decreases the aggressiveness of incoming impatient (patient) traders.

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**TABLE I**  
**Sample Statistics: Book and Activity**

This table provides average daily descriptive statistics on the 36 stocks in our sample, from July to December 2000. “Quote midpoint” is the average between the best offer and bid quotes. “Spread” is the distance, in number of ticks, between the best ask and bid quotes. “Ask (Bid) depth” is the accumulated number of shares offered at the five best ask (bid) quotes on the LOB. “Ask (Bid) orders” is the accumulated number of limit orders supporting the best ask (bid) quotes on the book. Ask<sub>1</sub>-Ask<sub>5</sub> (Bid<sub>1</sub>-Bid<sub>5</sub>) is the distance, in number of ticks, between the first and the fifth ask (bid) quotes on the book. “Daily Vol./1000 (Trades)” is the daily average share volume standardized by 1000(number of trades). The tick is 0.01 euros for all stocks and during all the sample period.

	Quote Midpoint	Spread (# ticks)	Ask Depth (Book)	Bid Depth (Book)	Ask Orders (Book)	Bid Orders (Book)	Ask <sub>1</sub> -Ask <sub>5</sub> (# ticks)	Bid <sub>1</sub> -Bid <sub>5</sub> (# ticks)	Daily Vol./1000	Daily Trades
ACR	9.30	3.17	10571.1	14832.1	18.36	11.84	5.83	5.78	277.85	370.48
ACS	27.11	13.70	4028.2	4392.9	7.01	7.69	19.22	18.79	133.83	249.15
ACX	32.09	13.07	3701.3	3926.0	8.03	7.40	18.91	19.57	175.34	328.65
ALB	27.55	19.03	3083.9	3232.3	6.31	6.44	23.59	21.30	136.75	188.77
ALT	16.31	4.05	12583.4	11611.8	8.60	12.94	8.05	9.07	1131.46	773.14
AGS	14.19	6.63	5316.6	5719.1	7.47	7.75	11.24	11.29	171.98	232.81
AMS	10.23	2.84	14416.6	16484.7	17.03	12.66	6.33	6.14	1177.81	924.65
ANA	38.48	14.68	2955.1	2883.1	7.20	7.01	22.24	21.73	125.52	288.21
AUM	16.63	8.90	6913.5	6626.0	7.69	9.65	12.75	18.70	102.09	76.23
BBV	16.07	1.71	84451.5	53025.4	13.90	39.14	4.84	4.96	6974.52	2023.90
BKT	44.19	11.73	3694.6	3734.3	9.17	7.99	18.67	16.34	224.68	559.02
CAN	20.97	12.06	8585.1	5853.9	6.45	8.07	15.58	18.93	146.01	148.24
CTG	18.94	7.29	6700.7	6860.1	8.53	8.99	10.93	10.97	372.38	369.15
DRC	9.94	3.60	18047.6	11783.3	9.62	15.56	6.69	7.81	624.81	440.19
ELE	20.80	2.45	24505.2	22732.6	10.07	12.75	6.34	6.34	3099.08	1496.06
FCC	19.56	8.63	5168.4	5081.2	8.01	8.35	13.52	13.90	183.95	322.99
FER	13.92	4.96	5974.4	6629.5	9.79	10.07	8.90	8.74	191.16	396.99
GPP	4.40	1.71	42577.5	40534.4	20.56	20.38	4.45	4.50	1107.38	620.10
IBE	13.80	2.57	31215.0	27039.0	11.22	15.85	5.74	6.20	2112.56	758.00
IDR	17.81	5.87	5819.6	5662.0	9.01	9.49	10.07	9.64	290.02	530.90
MAP	18.27	12.12	6629.1	5302.8	7.10	10.03	16.58	21.56	130.70	116.61
NHH	13.09	6.26	11189.7	9085.4	7.43	9.29	10.02	11.47	357.15	232.24
POP	34.72	8.57	8096.0	5174.1	7.43	12.55	13.66	14.05	395.66	463.60
PRS	23.68	7.95	5207.0	5825.4	8.76	11.72	12.52	14.06	382.35	554.59
REE	10.66	4.49	7034.9	9465.6	10.03	9.66	7.75	7.69	160.62	279.86
REP	20.32	2.41	25296.6	24654.2	13.76	12.37	6.14	5.99	3528.20	1655.46
SCH	11.45	1.34	178610.4	115052.2	28.81	97.43	4.33	4.31	9719.32	2962.41
SGC	33.37	12.24	3056.1	3041.5	8.58	7.21	18.59	17.10	202.47	545.57
SOL	10.92	4.70	7633.1	8448.2	9.47	8.42	8.27	7.89	280.60	292.52
TEF	21.90	1.56	65666.8	56251.7	23.83	19.05	4.90	4.67	19714.10	6608.87
TPZ	4.92	1.60	50389.1	68614.1	40.60	20.30	4.45	4.38	1433.03	847.68
TRR	34.53	4.75	8983.2	8675.3	15.11	11.48	9.59	8.37	2935.99	4596.82
TPI	8.83	2.41	14769.5	17494.5	17.24	12.05	5.61	5.39	1133.28	1008.90
UNF	20.47	4.40	14094.7	19545.4	8.21	9.20	8.89	7.72	768.06	413.85
VAL	6.71	3.01	14156.4	12739.4	10.09	11.35	5.95	6.49	334.15	253.67
ZEL	34.95	4.25	6826.7	5900.9	10.71	11.15	7.78	7.52	865.26	1776.36
Average	19.47	6.41	20220.79	17608.74	11.98	14.26	10.53	10.81	1697.23	936.30
Std. Dev.	(10.07)	(4.53)	(32720.8)	(23084.8)	(7.13)	(15.41)	(5.46)	(5.69)	(3677.81)	(1324.33)



TABLE II  
Statistics: Aggressiveness

This table provides general statistics on order aggressiveness for the 36 SSE-listed stocks in our sample, from July to December 2000. We classify orders in terms of 7 categories of aggressiveness (C1 to C7). C1 are cancellations. C2 are limit orders to sell (buy) above (below) the best ask (bid) quotes. C3 are limit orders to sell (buy) hitting the best ask (bid) quote. C4 are limit orders within the best quotes. C5 are market orders for a lower size than the depth available at the best quote on the opposite side of the book. C6 are totally or partially executed orders that consume (only) the best quote on the opposite side of the book. C7 are totally or partially executed orders that consume more than one level of quotes on the opposite side of the book. In Panel A we report the percentage of all seven categories of orders over all the orders submitted for the 36 stocks in the sample. We provide the distribution of all orders (buyer plus seller-initiated) and also the distribution of buyer-initiated and seller-initiated orders separately. In Panel B, we report similar statistics for each category of buyer-initiated and seller-initiated orders but this time over the total number of buyer or seller-initiated orders submitted, respectively.

	Cancellat.	Limit Orders			Small	Market	Large	Obs.
		Ab./Bel.	At	Within	M.O.	to Limit	M.O.	
A: Type/All orders	(C1)	(C2)	(C3)	(C4)	(C5)	(C6)	(C7)	
All	14.41	13.45	11.05	10.89	40.39	6.07	3.75	7971432
Buyer initiated	7.49	6.93	5.69	5.73	21.37	3.04	1.81	4150054
Seller initiated	6.92	6.52	5.36	5.16	19.02	3.02	1.94	3821378
B: Type/Signed orders								
Buyer initiated	14.39	13.31	10.93	11.01	41.05	5.85	3.47	4150054
Seller initiated	14.43	13.59	11.19	10.76	39.67	6.31	3.77	3821378

TABLE III

## First Stage of the SOP Model: Estimates and marginal probabilities

This table summarizes the estimation of the first stage of a sequential ordered probit (SOP) model for order aggressiveness with two stages. In this first stage, the dependent variable has three levels of aggressiveness: cancellations (withdrawal of liquidity), limit orders (provision of liquidity), and market orders (consumption of liquidity). In the second stage, the trader that has chosen to submit a limit order has to decide whether to place the limit order away from the best quotes, at the best quotes, or within the best quotes; the trader that chooses to submit a market order has to decide the size of his/her order: less volume than available at the best quote on the opposite side of the book, all that is available at the best quote on the opposite side of the book, or more volume than available at the best quote on the opposite side of the book. The estimation of the second stage is summarized in Table V. We report the median of the estimated coefficients for the 36 stocks in the sample, the percentage of statistically significant coefficients, and the percentage of statistically significant and positive coefficients. We provide separated results for buyer initiated orders and seller initiated orders. Additionally, we provide cross-sectional average marginal probabilities evaluated at the mean of the regressors. The marginal probabilities (x1000) measure the expected increase in the probability of each category after a marginal increase in a given regressor. The regressors, defined with respect to an incoming order, are: (1) Computed using the best ask and bid quotes: the bid-ask spread ( $SPR$ ), the number of orders on the same side of the market ( $NS^I$ ), and the number of orders on the opposite side of the market ( $NO^I$ ). (2) Computed using from the 2<sup>nd</sup> to the 5<sup>th</sup> best quotes: the accumulated number of orders on the same side of the market  $NS^{25}$ , the accumulated number of orders on the opposite side of the market  $NO^{25}$ . (3) The distance between the best and the second best (the second best and fifth best) quotes on the same side of the market  $LS^{12}$  ( $LS^{25}$ ), the distance between the best and the second best (the second best and fifth best) quotes on the opposite side of the market  $LO^{12}$  ( $LO^{25}$ ). All models include one lag of the dependent variable. All the statistics are calculated across the 36 stocks in the sample.

1 <sup>st</sup> Stage - Withdrawing, providing or consuming liquidity										
Sellers	Agr(-1)	$SPR$	$NS^I$	$NO^I$	$NS^{25}$	$NO^{25}$	$LS^{12}$	$LO^{12}$	$LS^{25}$	$LO^{25}$
Median Coef.	0.2072	-0.0167	0.0279	-0.0332	0.0040	-0.0035	-0.0074	0.0215	0.0026	-0.0057
Significant (%)	100	94.44	97.22	91.67	72.22	52.78	63.89	94.44	50.00	61.11
Sig. & Positive (%)	100	0.00	97.22	2.78	69.44	8.33	25.00	94.44	27.78	16.67
Buyers										
Median Coef.	0.1859	-0.0203	0.0495	-0.0220	0.0056	-0.0012	-0.0155	0.0262	-0.0066	-0.0059
Significant (%)	100	100.00	94.44	88.89	88.89	58.33	63.89	94.44	69.44	50.00
Sig. & Positive (%)	100	0.00	91.67	0.00	83.33	11.11	30.56	94.44	27.78	13.89
Marginal probabilities (cross-sectional means)										
Sellers	Agr(-1)	$SPR$	$NS^I$	$NO^I$	$NS^{25}$	$NO^{25}$	$LS^{12}$	$LO^{12}$	$LS^{25}$	$LO^{25}$
Withdrawing	-38.607	8.226	-8.362	-1.045	-1.693	0.251	2.180	-5.399	0.757	0.234
Providing liquidity	-26.688	6.294	-3.937	-0.329	-0.765	0.158	2.604	-3.725	1.197	0.494
Consuming liquidity	65.296	-14.520	12.299	1.374	2.458	-0.409	-4.783	9.123	-1.954	-0.728
Buyers										
Withdrawing	-34.735	9.760	-11.952	-0.034	-2.764	0.185	2.302	-6.582	1.173	0.144
Providing liquidity	-18.223	6.218	-3.181	0.353	-0.666	0.161	2.757	-4.254	1.224	0.118
Consuming liquidity	52.958	-15.978	15.134	-0.319	3.430	-0.346	-5.058	10.836	-2.396	-0.263

TABLE IV  
First Stage of the SOP Model: Performance

This table summarizes the results of an in-sample goodness-of-fit analysis and an out-of-sample predictive-ability analysis of three different specifications of the first stage of a sequential ordered probit (SOP) model for order aggressiveness. In its first stage, the dependent variable has three levels of aggressiveness: cancellations (withdrawal of liquidity), limit orders (provision of liquidity), and market orders (consumption of liquidity). In the second stage, the trader that has chosen to submit a limit order has to decide whether to place the limit order away from the best quotes, at the best quotes, or within the best quotes; the trader that chooses to submit a market order has to decide the size of his/her order: less volume than available at the best quote on the opposite side of the book, all that is available at the best quote on the opposite side of the book, or more volume than available at the best quote on the opposite side of the book. The three specifications considered are: the Baseline Model (BM), which only includes the first lag of the dependent variable in the set of explanatory variables; the Best Quotes Model (BQM), which adds variables computed from the best quotes of the book to the BM model; the Complete Book Model (CBM), which adds variables computed using from the 2<sup>nd</sup> to the 5<sup>th</sup> best quotes of the book to the BQM. The regressors computed using the best quotes are: the bid-ask spread (*SPR*), the number of orders on the same side of the market (*NS<sup>s</sup>*), the number of orders on the opposite side of the market (*NO<sup>s</sup>*). The regressors computed using the additional 4 quotes available of the book are: the accumulated number of orders on the same side of the market *NS<sup>25</sup>*, the accumulated number of orders on the opposite side of the market *NO<sup>25</sup>*, the distance between the best and the second best (the second best and fifth best) quotes on the same side of the market *LS<sup>12</sup>* (*LS<sup>25</sup>*), the distance between the best and the second best (the second best and fifth best) quotes on the opposite side of the market *LO<sup>12</sup>* (*LO<sup>25</sup>*). The in-sample analysis uses data from July to November 2000 and the out-of-sample analysis uses data from December 2000. The table reports the in-sample adjusted pseudo-R<sup>2</sup>s of McFadden (1973), Maddala (1983) with the Cragg-Uhler (1970) correction, Aldrich-Nelson (1984) with the Veall-Zimmermann (1992) correction, and McKelvey-Zavoina (1975). The out-of-sample adjusted McKelvey-Zavoina pseudo-R<sup>2</sup> is also provided. Finally, the table provides: (1) the percentage of stocks for which a given model is the best against using relative frequencies to predict the aggressiveness of the incoming order; (2) the percentage of stocks for which the CBM and the BQM outperform the BM on the basis that they usually allocate higher probabilities to the actual event than BM, and (3) the percentage of stocks for which the CBM outperforms the BQM on the basis of the same prediction rule.

Sequential Ordered Probit Model						
1st Stage: Withdrawing, consuming or providing liquidity						
In-sample Adjusted Pseudo-R <sup>2</sup> s		Sellers		Buyers		
BM Pseudo-R <sup>2</sup>						
McF		0.0097		0.0079		
MadCU		0.0220		0.0181		
AN		0.0283		0.0233		
MZ		0.0241		0.0198		
BQM (% increase over BM)						
McF		52.55		83.49		
MadCU		51.87		82.55		
AN		50.94		81.74		
MZ		51.68		82.75		
CBM (% increase over BQM)						
McF		49.80		41.91		
MadCU		51.48		43.06		
AN		51.17		42.60		
MZ		52.40		42.57		
Out-sample Adjusted Pseudo-R <sup>2</sup> (MZ)		Sellers		Buyers		
BM Pseudo-R <sup>2</sup>		0.0194		0.0156		
BQM (% increase over BM)		108.96		141.22		
CBM (% increase over BQM)		31.39		40.11		
Out-sample comparison		CBM	BQM	BM	CBM	BQM
Best model against the relative frequency		47.22	22.22	30.56	47.22	16.67
Better performance than the BM		100	97.22		97.22	100
Better performance than the BQM		94.44			97.22	

**TABLE V**  
**Second Stage of the SOP Model: Estimates and marginal probabilities**

This table summarizes the estimation of the second stage of a sequential ordered probit (SOP) model for order aggressiveness with two stages. In the first stage, the dependent variable has three levels of aggressiveness: withdrawal of liquidity, provision of liquidity, and consumption of liquidity. The estimation of the first stage is reported in Table III. In the second stage, the liquidity provider (Panel A) has to decide whether to place the limit order away from the best quotes, at the best quotes, or within the best quotes; the liquidity consumer (Panel B) has to decide the size of his/her market order: less volume than available at the best quote on the opposite side of the book, all that is available at the best quote on the opposite side of the book, or more volume than available at the best quote on the opposite side of the book. A positive estimated coefficient means that the associated explanatory variable is positively related to order aggressiveness. We report the median estimated coefficient for the 36 stocks in the sample, the percentage of statistically significant coefficients and the percentage of statistically significant and positive coefficients. Additionally, we provide cross-sectional average marginal probabilities evaluated at the mean of the regressors. The marginal probabilities measure the expected increase in the probability of each category after a marginal increase in a given regressor. We provide separated results for buyer initiated orders and seller initiated orders. The regressors, defined with respect to an incoming order, are: (1) Computed using the best ask and bid quotes: the bid-ask spread ( $SPR$ ), the number of orders stored on the same side of the book ( $NS^1$ ), the number of orders stored on the opposite side of the book ( $NO^1$ ). (2) Computed using from the 2<sup>nd</sup> to the 5<sup>th</sup> best quotes: the accumulated number of orders on the same side of the market ( $NS^{25}$ ), the accumulated number of orders on the opposite side of the market ( $NO^{25}$ ). (3) The distance between the best and the second best (the second best and fifth best) quotes on the same side of the market  $LS^{12}$  ( $LS^{25}$ ), the distance between the best and the second best (the second best and fifth best) quotes on the opposite side of the market  $LO^{12}$  ( $LO^{25}$ ). All models include one lag of the dependent variable.

Panel A: 2nd Stage - Limit order traders (Patient Traders)

Sellers	Agr(-1)	$SPR$	$NS^1$	$NO^1$	$NS^{25}$	$NO^{25}$	$LS^{12}$	$LO^{12}$	$LS^{25}$	$LO^{25}$
Median Coef.	0.1017	0.0201	0.0733	0.0032	-0.0063	0.0059	-0.0838	-0.0074	-0.0081	0.0099
Significant (%)	94.44	88.89	88.89	8.33	91.67	22.22	94.44	16.67	66.67	19.44
Sig. & Positive (%)	94.44	88.89	88.89	8.33	0.00	22.22	0.00	2.78	2.78	13.89
<b>Buyers</b>										
Median Coef.	0.0966	0.0167	0.0934	-0.0015	-0.0076	0.0030	-0.0888	-0.0149	-0.0062	0.0105
Significant (%)	97.22	91.67	97.22	5.56	94.44	33.33	97.22	30.56	52.78	30.56
Sig. & Positive (%)	97.22	91.67	97.22	2.78	0.00	27.78	0.00	5.56	0.00	16.67

Marginal probabilities (cross-sectional means) (x1000)

Sellers	Agr(-1)	$SPR$	$NS^1$	$NO^1$	$NS^{25}$	$NO^{25}$	$LS^{12}$	$LO^{12}$	$LS^{25}$	$LO^{25}$
Above the best quote	-33.986	-11.262	-21.943	0.315	3.252	-0.529	40.913	0.752	3.219	-1.496
At the best quote	-0.688	2.111	-1.741	0.348	0.396	-0.036	-5.711	0.358	-0.060	0.451
Inside the spread	34.674	9.150	23.684	-0.663	-3.648	0.565	-35.203	-1.110	-3.159	1.045
<b>Buyers</b>										
Below the best quote	-32.701	-9.672	-28.694	-0.283	3.346	-0.833	43.119	2.673	1.681	-0.562
At the best quote	-3.144	1.429	-4.307	-0.004	0.673	-0.149	-5.068	-0.159	0.091	0.274
Inside the spread	35.845	8.242	33.001	0.287	-4.020	0.982	-38.051	-2.513	-1.773	0.289

Panel B: 2nd Stage - Market order traders (Impatient Traders)

Sellers	Agr(-1)	$SPR$	$NS^1$	$NO^1$	$NS^{25}$	$NO^{25}$	$LS^{12}$	$LO^{12}$	$LS^{25}$	$LO^{25}$
Median Coef.	0.1144	0.0424	-0.0099	-0.2878	-0.0020	0.0078	0.0123	-0.0212	0.0178	-0.0106
Significant (%)	97.22	66.67	27.78	100	58.33	63.89	36.11	63.89	66.67	55.56
Sig. & Positive (%)	97.22	66.67	2.78	0	8.33	61.11	33.33	0	63.89	5.56
<b>Buyers</b>										
Median Coef.	0.1079	0.0304	-0.0306	-0.2401	-0.0058	0.0079	0.0220	-0.0269	0.0145	-0.0076
Significant (%)	94.44	86.11	38.89	97.22	77.78	66.67	58.33	80.56	61.11	27.78
Sig. & Positive (%)	91.67	86.11	5.56	0	5.56	63.89	52.78	0	58.33	2.78

Marginal probabilities (cross-sectional means) (x1000)

Sellers	Agr(-1)	$SPR$	$NS^1$	$NO^1$	$NS^{25}$	$NO^{25}$	$LS^{12}$	$LO^{12}$	$LS^{25}$	$LO^{25}$
Non aggressive	-30.580	-14.058	2.305	78.642	0.721	-1.773	-2.709	5.438	-3.822	1.853
Market-to-limit	14.876	7.802	-1.048	-38.792	-0.341	0.822	1.472	-2.733	2.111	-0.961
Aggressive	15.704	6.256	-1.257	-39.849	-0.380	0.951	1.237	-2.704	1.711	-0.892
<b>Buyers</b>										
Non aggressive	-30.501	-16.578	5.159	71.845	2.758	-1.857	-4.369	9.654	-3.537	1.368
Market-to-limit	15.790	9.805	-2.535	-36.542	-1.426	0.909	2.502	-5.491	2.041	-0.801
Aggressive	14.711	6.772	-2.624	-35.303	-1.331	0.948	1.866	-4.164	1.495	-0.568

TABLE VI  
Second Stage of the SOP Model: Performance

This table summarizes the results of an in-sample goodness-of-fit analysis and an out-of-sample predictive-ability analysis for three different specifications of a sequential ordered probit (SOP) model of order aggressiveness. In its first stage, the dependent variable has three levels of aggressiveness: cancellations (withdrawal of liquidity), limit orders (provision of liquidity), and market orders (consumption of liquidity). In the second stage, the trader that has chosen to submit a limit order has to decide whether to place the limit order away from the best quotes, at the best quotes, or within the best quotes; the trader that chooses to submit a market order has to decide the size of his/her order: less volume than available at the best quote on the opposite side of the book, all that is available at the best quote on the opposite side of the book, or more volume than available at the best quote on the opposite side of the book. The three specifications are: the Baseline Model (BM), which only includes the first lag of the dependent variable in the set of explanatory variables; the Best Quotes Model (BQM), which adds variables computed from the best quotes of the book to the BM model; the Complete Book Model (CBM), which adds variables computed using from the 2<sup>nd</sup> to the 5<sup>th</sup> best quotes of the book to the BQM. The regressors computed using the best quotes are: the bid-ask spread ( $SPR$ ), the number of orders on the same side of the market ( $NS^l$ ), and the number of orders on the opposite side of the market ( $NO^l$ ). The regressors computed using the additional 4 quotes available of the book are: the accumulated number of orders on the same side of the market  $NS^{25}$ , the accumulated number of orders on the opposite side of the market  $NO^{25}$ , the distance between the best and the second best (the second best and fifth best) quotes on the same side of the market  $LS^{12}$  ( $LS^{25}$ ), the distance between the best and the second best (the second best and fifth best) quotes on the opposite side of the market  $LO^{12}$  ( $LO^{25}$ ). The in-sample analysis uses data from July to November 2000 and the out-of-sample analysis uses data from December 2000. The table reports the in-sample adjusted pseudo- $R^2$ s of McFadden (1973), Maddala (1983) with the Cragg-Uhler (1970) correction, Aldrich-Nelson (1984) with the Veall-Zimmermann (1992) correction, and McKelvey-Zavoina (1975). The out-of-sample adjusted McKelvey-Zavoina pseudo- $R^2$  is also provided. Finally, the table provides: (1) the percentage of stocks for which a given model is the best against using relative frequencies to predict the aggressiveness of the incoming order (2) the percentage of stocks for which the CBM and the BQM outperform the BM on the basis that they usually allocate higher probabilities to the actual event than BM, and (3) the percentage of stocks for which the CBM outperforms the BQM on the basis of the same prediction rule. Table IV provides the results for the first stage of the SOP model.

2nd Stage Sequential Ordered Probit Model												
	Passive Traders (Liquidity Providers)						Active Traders (Liquidity Consumers)					
In-sample Adjusted Pseudo-R <sup>2</sup> s	Sellers			Buyers			Sellers			Buyers		
BM Pseudo-R <sup>2</sup>												
McF	0.0037			0.0031			0.0019			0.0022		
MadCU	0.0092			0.0078			0.0033			0.0041		
AN	0.0119			0.0100			0.0043			0.0054		
MZ	0.0107			0.0087			0.0043			0.0053		
BQM (% increase over BM)												
McF	131.04			177.32			1095.97			1005.21		
MadCU	134.62			176.86			1104.73			976.90		
AN	134.34			175.29			1088.45			956.08		
MZ	143.11			197.91			3739.82			3128.25		
CBM (% increase over BQM)												
McF	272.94			221.91			25.78			34.43		
MadCU	259.05			213.73			24.14			34.78		
AN	250.48			207.29			23.36			33.62		
MZ	267.34			202.79			1.85			13.54		
Out-sample Adjusted Pseudo-R <sup>2</sup> (MZ)	Sellers-M2			Buyers-M2			Sellers-M2			Buyers-M2		
BM Pseudo-R <sup>2</sup>	0.0107			0.0086			0.0054			0.0772		
BQM (% increase over BM)	126.73			152.47			2097.78			1258.31		
CBM (% increase over BQM)	334.57			325.53			7.82			21.88		
Out-sample comparison	CBM	BQM	BM	CBM	BQM	BM	CBM	BQM	BM	CBM	BQM	BM
Best model against the relative frequency	91.67	8.33	0.00	88.89	11.11	0.00	38.89	22.22	38.89	27.78	19.44	52.78
Better performance than the BM	100	97.22		100	100		44.44	22.22		47.22	27.78	
Better performance than the BQM	100			100			38.89			50.00		

**TABLE VII**  
**SOP Model vs. OP Model: Performance**

This table compares the performance of a two-stage sequential ordered probit (SOP) model for order aggressiveness with a one-stage ordered probit model (OP) model. In the first stage of the SOP model, the dependent variable has three levels of aggressiveness: cancellations (withdrawal of liquidity), limit orders (provision of liquidity), and market orders (consumption of liquidity). In the second stage, the trader that has chosen to submit a limit order has to decide whether to place the limit order away from the best quotes, at the best quotes, or within the best quotes; the trader that chooses to submit a market order has to decide the size of his/her order: less volume than available at the best quote on the opposite side of the book, all that is available at the best quote on the opposite side of the book, or more volume than available at the best quote on the opposite side of the book. The OP model considers seven categories of order aggressiveness: cancellations (C1), limit orders away from the best quotes (C2), limit orders at the quotes (C3), limit orders inside the quotes (C4), non-aggressive market orders (C5), market-to-limit orders (C6), and aggressive market orders (C7). Both models include the same set of explanatory variables: the first lag of the dependent variable, the bid-ask spread ( $SPR$ ), the number of orders on the same side of the market ( $NS^i$ ), the number of orders on the opposite side of the market ( $NO^i$ ), the accumulated number of orders on the same side of the market  $NS^{25}$ , the accumulated number of orders on the opposite side of the market  $NO^{25}$ , the distance between the best and the second best (the second best and fifth best) quotes on the same side of the market  $LS^{12}$  ( $LS^{25}$ ), the distance between the best and the second best (the second best and fifth best) quotes on the opposite side of the market  $LO^{12}$  ( $LO^{25}$ ). The in-sample analysis uses data from July to November 2000 and the out-of-sample analysis uses data from December 2000. The table reports the number of stocks (up to 36) and the percentage of observations for which the SOP model outperforms the OP model in the sense that the SOP model it allocates a higher probability to the actual event than the OP.

Buys					Sells				
In sample					In sample				
		SOP					SOP		
		vs. OP	Obs.				vs. OP	Obs.	
	Stocks	36	3506233			Stocks	36	3242140	
	% Obs.	60.28%				% Obs.	59.63%		
Out of sample					Out of sample				
	Stocks	35	552053			Stocks	36	513959	
	% Obs.	58.72%				% Obs.	58.60%		
Buys - Aggressiveness					Sells - Aggressiveness				
In sample					In sample				
	C1	Stocks	22	515523		C1	Stocks	19	474179
		% Obs.	48.58%				% Obs.	47.52%	
	C2	Stocks	32	474259		C2	Stocks	33	446853
		% Obs.	52.70%				% Obs.	53.92%	
	C3	Stocks	36	389114		C3	Stocks	36	365332
		% Obs.	62.63%				% Obs.	62.66%	
	C4	Stocks	36	388340		C4	Stocks	36	344202
		% Obs.	60.73%				% Obs.	60.27%	
	C5	Stocks	36	1413969		C5	Stocks	36	1278047
		% Obs.	63.88%				% Obs.	62.79%	
	C6	Stocks	32	206444		C6	Stocks	35	204115
		% Obs.	64.57%				% Obs.	61.24%	
	C7	Stocks	36	118584		C7	Stocks	36	129412
		% Obs.	81.69%				% Obs.	79.60%	
Out of sample					Out of sample				
	C1	Stocks	29	92207		C1	Stocks	28	87503
		% Obs.	52.41%				% Obs.	52.14%	
	C2	Stocks	32	78144		C2	Stocks	32	72537
		% Obs.	54.70%				% Obs.	53.84%	
	C3	Stocks	35	64379		C3	Stocks	34	62124
		% Obs.	63.57%				% Obs.	70.00%	
	C4	Stocks	35	68622		C4	Stocks	35	66836
		% Obs.	60.43%				% Obs.	61.23%	
	C5	Stocks	23	193036		C5	Stocks	22	168404
		% Obs.	57.32%				% Obs.	55.93%	
	C6	Stocks	36	36124		C6	Stocks	32	36902
		% Obs.	67.51%				% Obs.	62.31%	
	C7	Stocks	35	19541		C7	Stocks	34	19653
		% Obs.	80.19%				% Obs.	75.84%	